# Lesson 11-1

### **Mathematical Patterns**

Lesson Objectives	NAEP 2005 Strand: Algebra			
<b>V</b> Identifying mathematical patterns	Topic: Patterns, Relations, and Functions			
Using a formula for finding the <i>n</i> th term in a sequence	Local Standards:			

### Vocabulary

A sequence is

A term in a sequence is \_\_\_\_\_

A recursive formula

An explicit formula

### Examples

**1** Physics Suppose you drop a ball from a height of 100 cm. It bounces back to 80% of its previous height. About how high will it go after its fifth bounce?

Α.	100 cm	<b>B.</b> 80 cm	<b>C.</b> 32.8 cm	<b>D.</b> 26.2 ci	n
		Orig	inal height of ball	$:100 \text{ cm} \rightarrow$	
	After f	irst bounce: 80%	6  of  100 = 0.80(10)	$(00) = 80 \rightarrow$	
		After 2nd b	oounce: 0.80(80) =		
	Aft	ter 3rd bounce:	0.80(	$\rightarrow$	
	After 4	th bounce: 0.80		→	
А	fter 5th bou	ince: 0.80(		<b>→</b>	
TI	ne ball will	rebound about 3	32.8 cm after the f	ifth bounce.	

The correct choice is C.

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a. Describe the pattern that allows you to find the next term in the sequence

2, 6, 18, 54, 162, .... Write a recursive formula for the sequence.



**b.** Find the sixth and seventh terms in the sequence.

Since  $a_5 = 162, a_6 = 162 \cdot 3 =$  , and  $a_7 =$  .

**c.** Find the value of  $a_{10}$  in the sequence.

**O** Using a Recursive Formula

The term 
$$a_{10}$$
 is the tenth term.  $a_{10} = a_9 \cdot 3 = (a_8 \cdot 3) \cdot 3 = ((a_7 \cdot 3) \cdot 3) \cdot 3 = (((a_7 \cdot 3) \cdot 3) \cdot 3) \cdot 3 = ((a_7 \cdot$ 

# **Quick Check**

- **1.** Use the information from Example 1.
  - **a.** About how high will the ball rebound after the eighth bounce?
- **b.** After what bounce will the rebound height be less than 11 cm?



**2.** Use the sequence from Example 2. Find terms  $a_{11}$  and  $a_{13}$  in the sequence.

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## Example

**Geometry** The spreadsheet shows the perimeters of regular pentagons with sides from 1 to 4 units long. The numbers in each row form a sequence.

	А	В	С	D	Ε	F
1		a <sub>1</sub>	a <sub>2</sub>	a <sub>3</sub>	a <sub>4</sub>	
2	Length of a Side	1	2	3	4	
3	Perimeter	5	10	15	20	

**a.** For each sequence, find the next term  $(a_5)$  and the twentieth term  $(a_{20})$ .

In the sequence in row 2, each term is the same as its subscript. Therefore,  $a_5 = |$  and  $a_{20} = |$ 

In the sequence in row 3, each term is times its subscript. Therefore, and  $a_{20} = 5$ |) =|) = $a_5 = 5(|$ 

**b.** Write an explicit formula for each sequence.

The explicit formula for the sequence in row 2 is . The explicit =formula for the sequence in row 3 is =

# **Quick Check**

3. The spreadsheet shows the perimeters of squares with sides from 2 to 12 units long.

	А	В	С	D	Ε	F	G	Η
1		a <sub>1</sub>	a <sub>2</sub>	a <sub>3</sub>	a <sub>4</sub>	a <sub>5</sub>	a <sub>6</sub>	•••
2	Length of a Side	2	4	6	8	10	12	
3	Perimeter	8	16	24	32	40	48	

- **a.** Write the first six terms in the sequence showing the areas of the squares. Then find  $a_{20}$ .
- **b.** Write an explicit formula for the sequence from part (a).



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